## Convex Hulls

Math 282 Computational Geometry

1. Let $S$ be a set of points in the plane. Given points $a$ and $b$ in $S$, how would you determine whether the segment $a b$ is part of the convex hull $\operatorname{conv}(S)$ ?

Here is a sample set of points $S$ :

2. Given the coordinates of all points in $S$, how would you program a computer to determine whether a particular pair of points in $S$ are endpoints of an edge of $\operatorname{conv}(S)$ ?
Here is a sample set of points, specified by coordinates:

$$
\begin{aligned}
& (0.9,4.7) \\
& (1.1,9.3) \\
& (6.6,2.5) \\
& (8.2,1.8) \\
& (6.8,8.1) \\
& (4.7,7.3) \\
& (3.8,1.5) \\
& (5.0,2.9) \\
& (2.6,5.2) \\
& (5.9,6.4)
\end{aligned}
$$

3. Given the coordinates of all points in $S$, how would you program a computer to find all edges of $\operatorname{conv}(S)$ ?
4. How many operations would your algorithm require to find the convex hull of 10 points? ...of 100 points? ...of 1000 points?
